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Fraunhofer regime of operation for superconducting quantum interference filters

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Series arrays of superconducting quantum interference devices (SQUIDs) with incommensurate loop areas, so-called superconducting quantum interference filters (SQIFs), are investigated in the kilohertz and the gigahertz frequency range. In SQIFs made of high- T_c bicrystal junctions the flux-to-voltage response $\partial V/\partial \Phi$ is dominated by the variation in the critical current in the individual junctions (Fraunhofer-type) rather than by the SQUIDs interference. For a SQIF with 20 SQUID loops we find $\partial V/\partial \Phi = 40$ mV/ Φ_0 and a dynamic range of more than 60 dB in the kilohertz range. In the 1–2 GHz range the estimated power gain is 20 dB and the magnetic flux noise level is as low as $10^{-4}\Phi_0$. © 2008 American Institute of Physics. [DOI: 10.1063/1.3058759]

Microwave amplifiers based on superconducting quantum interference effects in two parallel connected Josephson junctions (JJs) (SQUID) (SQUID denotes superconducting quantum interference device) are characterized by a noise temperature close to the quantum limit (see, e.g., Refs. 1 and 2). SQUID amplifiers, as well as other Josephson devices without feedback, possess low saturation power, which is proportional to the characteristic voltage $V_0 = I_c R_n$, where I_c is the critical current and R_n is the normal state resistance of the JJ. For resistively shunted tunnel JJs made of low- T_c superconductors (LTS), V_0 (here R_n is the shunt resistance needed to avoid hysteresis) only reaches 200–300 μ V at $T = 4.2$ K (Ref. 2), while the bicrystal JJs made of high- T_c superconductors (HTS) can give $V_0 = 1$ mV at $T = 77$ K.³

The output signal and saturation power can be increased by using an array of JJs or SQUIDs. An increase in the output signal proportional to the number N of SQUIDs was demonstrated in an amplifier based on a series-connected array of LTS SQUIDs.⁴ Generally, however, the spread in I_c and R_n parameters of the HTS JJs is a pertinent problem that restricts the use of series-connected JJs or SQUID arrays. Superconducting quantum interference filters (SQIFs)—arrays of SQUIDs (series or parallel connected) with incommensurate SQUID-loop areas—accept much wider margins in parameter spread.^{5–7} For a SQIF with small normalized array loop inductances $l_i < 1$ (where $l_i = 2\pi I_c L_i/\Phi_0$, $\Phi_0 = h/2e$ is the magnetic flux quantum, I_c is the critical current, and L_i is the SQUID-loop inductance) and a suitably chosen distribution of loop sizes, the magnetic field to voltage response $V(H)$ is a nonperiodic function with a single narrow global minimum at $H = 0$. The contributions from the different SQUID loops are washed out, and the width of the $V(H)$ minimum is determined by the number of loops and the size of the largest SQUID loop.⁷ For short we will call this operational regime of the SQIF with a single $V(H)$ minimum at $H = 0$ the S -mode. Note that in the S -mode also the influence of the Fraunhofer-like $I_c(H)$ dependence in the individual JJs

is visible but may be neglected. Recently, HTS SQIFs have been studied for microwave amplification.^{8,9}

Sensitive magnetometers based on one-dimensional series arrays of HTS bicrystal JJs have been reported.¹⁰ Here both the Fraunhofer dependence of the critical current in the JJs, $I_c(H) = I_c(0) |\sin(\pi \Phi_J/\Phi_0)| / (\pi \Phi_J/\Phi_0)$ (where $\Phi_J = \mu_0 H a_J$ is the magnetic flux in a JJ with effective area a_J), and the flux focusing due to the geometry of the bicrystal JJ have to be taken into account. We call this operational regime the F -mode. A field-voltage transfer function $dV/d\mu_0 H = 7500$ V/T (μ_0 —vacuum permeability) was obtained for an array with $N = 105$ series-connected JJs.¹⁰ This compares well with the sensitivity of a LTS SQUID array with small spread of parameters.⁴

In this paper we investigate series-connected SQIF consisting of 20 HTS bicrystal SQUIDs with SQUID-loop inductances in the range of 15–300 pH. The width ($w = 10$ μ m) of the film forming both the JJs and the SQUID loops is much larger than the London penetration depth λ_L in YBa₂Cu₃O_x (YBCO). The external magnetic flux produced by the input signal coil induces circulating currents in the superconducting SQUID loops. Since $w \gg \lambda_L$ the current circulating along the inside edge of the SQUID loop is compensated by the current in the outer edge of the SQUID loop. The presence of the circulating current in the JJs provides better inductive coupling between the JJs and the input circuit and in turn increases the microwave amplification.

Bicrystal NdGaO₃ (NGO) substrates were used in the sample fabrication. NGO is characterized by a tolerable permittivity ($\epsilon = 25$) and fairly low microwave losses ($\tan \delta < 10^{-3}$). Devices were formed by ion-plasma and chemical etching of YBCO film deposited by dc sputtering at high oxygen pressure. The fabrication details of bicrystal JJs have been described elsewhere.³ Single loop SQUID and series-connected SQUID arrays⁸ were fabricated for comparison. Figure 1 shows the topology of a SQIF designed for use as microwave amplifier. The input line (Au film) was deposited over a SiO₂ insulator layer; the bottom layer is the YBCO film that forms the SQIF located inside the input line. The

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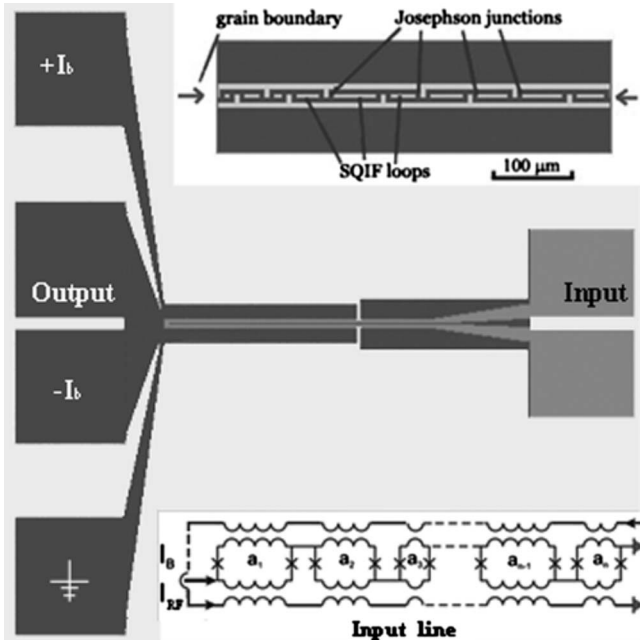


FIG. 1. Layout of a SQIF designed for microwave amplifier. It consists of 20 series-connected SQUID loops with areas in the range of $35\text{--}700\ \mu\text{m}^2$. The width w of the JJs is $10\ \mu\text{m}$. The input line circuit for the I_{rf} current consists of a top Au thin film (gray color) deposited over the SiO_2 buffer layer. The YBCO thin film is the bottom layer (dark color). The output circuit is a coplanar-line YBCO film with the SQIF junctions located along the bicrystal boundary. The top inset shows a zoomed view of the bottom layer with a part of the SQIF. The bottom inset shows a circuit with a SQIF and pick-up loop. I_b is dc bias current.

output voltage signal is taken directly from the SQIF.

We measured dc I - V and $V(H)$ curves at low frequency as well as the output noise power $P_n = k_b T_n \Delta f$ in the frequency range $f = 1\text{--}2\ \text{GHz}$. For the noise power measurements we used a cryogenic preamplifier with noise temperature $T_{A1} = (8 \pm 2)\ \text{K}$ and gain $G = 21\ \text{dB}$, followed by a room temperature amplifier with $T_{A2} = 130\ \text{K}$ and $G = 40\ \text{dB}$. The output voltage signal was simultaneously recorded by a spectrum analyzer and a quadratic detector integrated into the room amplifier.

From the $I_c(H)$ pattern measured on the reference SQUID with loop area $S = 35\ \mu\text{m}^2$ we estimate a loop inductance $L = (15 \pm 5)\ \text{pH}$.^{8,11} The estimated spread in critical currents of JJs in the SQIF was $\delta I/I_n \approx 30\%$. Using the mean value of $I_c = 100\ \mu\text{A}$ for JJs with width $w = 10\ \mu\text{m}$, we calculate the normalized inductances of the loops in the SQIF to be in the range $l_i = 4\text{--}90$.

Numerical simulations (using the PSCAN program)¹² of the $V(H)$ curve for SQIFs with different number of loops N are shown in Fig. 2. Experimental values of loop inductances as well as the Fraunhofer dependence of the JJ critical currents are taken into account. This leads to an aperiodic $V(H)$ response even for a single SQUID. The modulation of the side lobes is suppressed with increasing N . Dips due to both Fraunhofer modulations in junctions and SQUID interference can be seen for $N > 10$. Finally for $N = 20$ one observes a wide dip due to the Fraunhofer dependence of the critical currents of the JJs (F -mode) and a small, narrow zero dip due to the effect of the SQUID loops (S -mode). Note that taking into account a 30% spread of the critical currents I_{ci} of the JJs in the SQIF, the numerical simulation gives a decrease in both F - and S -mode amplitudes.

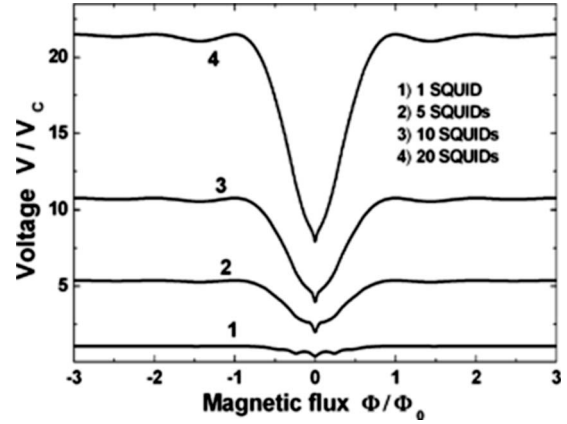


FIG. 2. Numerical simulation of the $V(H)$ response for SQIFs with different numbers of loops. The Fraunhofer dependence of the JJ critical currents is taken into account. For the SQIF the normalized inductances are in the range $l_i = 4\text{--}90$. For the single SQUID $l_i = 4$. Dips due to both Fraunhofer modulation in the junctions and the SQUID interference can be seen for $N > 10$.

Figure 3 shows a family of $V(H)$ responses of a SQIF with 20 loops plotted at different dc bias currents I_b . A single F -mode dip with small side voltage modulation is seen for all I_b . The inset shows a zoom-in of the central part. Besides the single S -mode dip predicted by numerical simulations (Fig. 2), additional dips produced by the SQUIDs response interference are observed. The width of the $V(H)$ dip is considerably larger than the dip in a SQIF operated in the S -mode.^{5-7,9} The width of the F -mode dip is well fitted using an effective JJ area $S_{\text{eff}} = 30\ \mu\text{m}^2$. This is larger than the evaluated area of JJ $w\lambda_L = 1.5\ \mu\text{m}^2$, where w is the JJ width and $\lambda_L = 0.15\ \mu\text{m}$ is the London penetration depth in YBCO. This observation is in agreement with a strong flux focusing effect in a bicrystal JJ (Ref. 13) when the magnetic field is applied perpendicular to the film. The expected value of the $V(H)$ response, $V_S = \sum V_{0i}$, should increase with the number N of SQIF loops, each contributing $V_{0i} = I_{ci} R_{ni}$. However, the experimental $V_S = 12\ \text{mV}$ turned out smaller than the estimated $\sum V_{0i} = 20\ \text{mV}$ for a SQIF with $N = 20$. For the SQIF

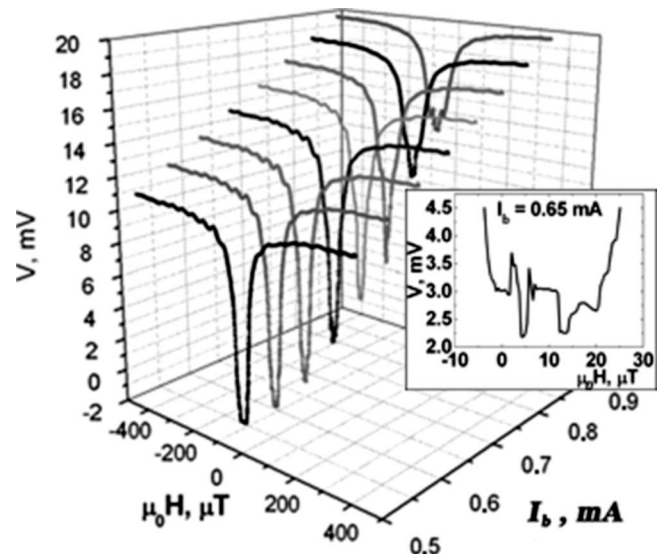


FIG. 3. Magnetic field-to-voltage response $V(H)$ of a SQIF array with 20 loops for different dc bias currents I_b . The measurements were made at $T = 4.2\ \text{K}$. For the structure with critical current $I_c = 560\ \mu\text{A}$, the maximum amplitude of dV/dH is observed at $I_b = 1.1 I_c$. The fine structure of the central part of the F -mode dip is shown in the inset.

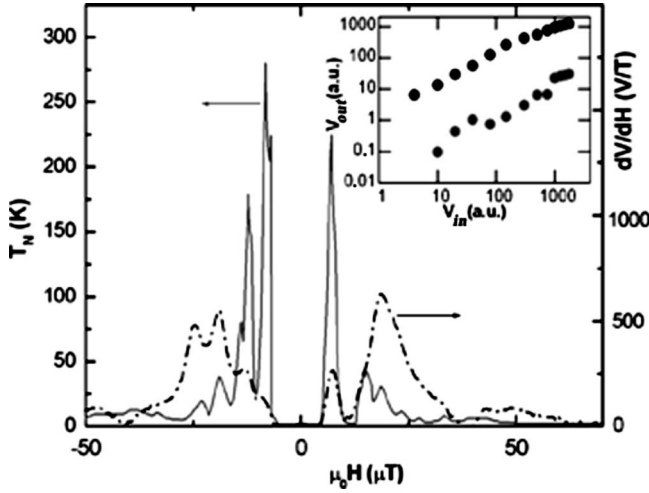


FIG. 4. Magnetic field dependence of the noise temperature $T_n(H)$ for a 20 loop SQIF in the frequency band $f=1-2$ GHz (solid line). The dash-dotted line shows the $dV/dH(H)$ dependence. The bias current is $I_b=1.25I_c$, $T=4.2$ K. The inset shows the dependence of the first (black points) and second harmonics (gray points) of the output signal V_{out} vs input signal V_{in} at frequency $f_{in}=900$ Hz.

operating in the F -mode we obtain $dV/d\Phi=40$ mV/ Φ_0 (and $dV/d\mu_0H=270$ V/T), while for the reference SQUID $dV/d\Phi=1$ mV/ Φ_0 .⁸ Thus for a SQIF made of HTS bicrystal JJs, the F -mode plays a predominant role in the $V(H)$ response.

The output noise temperature $T_n(H)$ measured in the frequency range $f=1-2$ GHz for a 20 loop SQIF is presented in Fig. 4. The output noise power is up to 15 dB above the background noise level. The measured output noise signal from the SQIF can be interpreted as an incoherent superposition of voltage spectral density of thermal fluctuations $S_V^T=\Sigma(8kTR_d^2/R_n)[1+1/2(I/I_c)^2]$ and voltage spectral density corresponding to contribution of magnetic flux conversion $S_V^\Phi=\Sigma(2kTL_n^2/R_n)(dV_n/d\Phi_n)^2$.^{14,15} For a bias current $I_b=1.25I_c$ and $R_d=30$ Ω at the $T_n(H)$ peak we get S_V^Φ/S_V^T proportional to $\max(I_i)/N>1$ [neglecting $R_{di}(H)$ and I_{ci} variation in the SQIF]. It indicates that the observed output noise signal is dominated by the magnetic flux conversion S_V^Φ rather than the thermal fluctuations S_V^T . With $dV/d\Phi=40$ mV/ Φ_0 , the SQIF is characterized by a flux sensitivity $\delta\Phi=10^{-4}\Phi_0$. Both the $dV/dH(H)$ and the $T_n(H)$ functions have complex dependences with several maxima. However, some of the $T_n(H)$ peaks are correlated with the dV/dH function. The side lobe modulation of the dV/dH [weakly seen in the $V(H)$ response] and the corresponding behavior of the $T_n(H)$ function may be caused by residual contributions from the SQUID-loop interference that could be increased by the asymmetry in the critical currents in large inductive SQUIDS ($I\gg 1$).¹⁶ Finally the complex behavior of the $T_n(H)$ function could be the result of the $R_d(H)$ dependence due to the scattering of the I_{ci} parameters.

In order to estimate the power gain $G=M^2(dV/d\Phi)^2/R_dR_s$,^{17,18} we take $R_s=50$ Ω as the microwave source resistance, the measured dynamic resistance $R_d=30$ Ω , and an estimated mutual coupling inductance $M=2.4\times 10^{-11}$ H, assuming a geometrical coupling coefficient $\alpha=0.2$ (for the SQIF layout shown in Fig. 1). Using the experimental value $dV/d\Phi=2\times 10^{13}$ s⁻¹ obtained from

measurements at low frequencies, we get a power gain $G=20$ dB.

In order to estimate the saturation power of the SQIF array, we measured the output signal at low frequencies $f=49$ Hz–90 kHz. The expected saturation power of non-coherently operating SQIF loops increases as the square root of N , $P_S\propto\sqrt{N}$.⁵⁻⁷ An analysis of the experimental data for the first and the second harmonic of the output signal response with an applied 900 Hz signal to the 20 loop SQIF biased at $I/I_c=1,1$ shows quasilinear dependence over 60 dB (see the inset in Fig. 4). We observed a signal distortion with the second harmonic amplitude of about 1% relative to of the first harmonic amplitude. Note that a similar harmonic distortion was reported for a LTS SQUID amplifier.¹⁸

Summarizing, we have fabricated and studied HTS SQIFs operating in the F -mode where the magnetic field-to-voltage response is mostly determined by a Fraunhofer dependence of the critical current of the individual JJs. The flux-to-voltage conversion factor in the F -mode is apparently lower than the factor expected in the originally suggested S -mode due to the smaller effective areas of the JJs than of the SQUID loops. Nevertheless our SQIF showed a power gain $G>1$ in the F -mode and a significant increase in saturation power and dynamic range.

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